

ASD-TR-68-19

AD 675643

COMPUTER PROGRAM FOR REDUCING STATIC PROPELLER TEST DATA

GERALD T. CAFARELLI

MATTHEW H. CHOPIN

TECHNICAL REPORT ASD-TR-68-19

JUNE 1968

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DEPUTY FOR ENGINEERING
AERONAUTICAL SYSTEMS DIVISION
AIR FORCE SYSTEMS COMMAND
WRIGHT-PATTERSON AIR FORCE BASE, OHIO

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FOREWORD

This report was prepared by the V/STOL Propulsion Branch, Directorate of Propulsion and Power Subsystems Engineering, Deputy for Engineering, Aeronautical Systems Division, under System 478A. Work was accomplished from July 1966 to November 1967. The authors served as project engineers.

This report was released by the authors in April 1968.

The authors wish to express their appreciation to Major Allan Gay, Directorate of Computation Services, Deputy for Engineering, for developing the computer program and applying the curve-fit technique to the data reduction as described in this report.

This technical report has been reviewed and is approved.

A handwritten signature in dark ink, appearing to read "James G. Barrett", is written over a horizontal line.

JAMES G. BARRETT
Technical Director
Directorate of Propulsion and
Power Subsystems Engineering

ABSTRACT

A computer program using a curve-fit technique was developed to reduce performance data obtained from static tests of aircraft propellers. The entire program is written in Fortran IV language for use on the IBM 7094 computer located at Wright-Patterson AFB, Ohio.

The program accepts static whirl rig test data (ie, raw RPM, horsepower, and thrust data) obtained at a fixed blade angle and reduces it into pertinent propeller relationships. The program first reduces the test data into various coefficients and computes the propeller tip Mach number. A curve fit technique then fits running curves through the test thrust and horsepower data points at the test tip Mach numbers. Intermediate horsepower and thrust values are determined from the fitted curves at selected Mach number increments, and all coefficients are recomputed. This results in a presentation of the reduced data in two forms, coefficients computed from the actual test data and coefficients obtained at specific constant Mach number increments from the fitted curves. The data is presented in tabular printout form. This is a general program and is written so that the order of the curve fit, the Mach number increment, the number of test data points and the Mach number range can be varied.

The entire program deck and all nonstandard subroutines are included. Detail instructions are provided which should allow the program to be used by technicians or students who are familiar with Fortran IV language.

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SECTION I

INTRODUCTION

This program was developed to reduce data accumulated during an extensive series of static tests of propellers for the XC-142A V/STOL aircraft conducted at Wright-Patterson Air Force Base, Ohio. These tests are described in detail in a report being prepared entitled "Propeller Static Performance Tests for V/STOL Aircraft." The program is complete in that it contains all non-standard subroutines.

The program reduces RPM and corrected horsepower and thrust data at any given blade angle and computes Power Coefficient (C_p), Thrust Coefficient (C_t), C_t/C_p , Figure of Merit (F.M.) and thrust/horsepower (TH/HP). Propeller tip Mach number is calculated using propeller diameter, RPM and ambient temperature. A curve fit technique is then employed to fit a running selected degree polynomial using least squares to NPHP (horsepower) or NPTH (thrust) consecutive test data points (see NAMELIST) at the test tip Mach numbers. In this case, a 2nd degree polynomial was fit to 6 consecutive data points. Intermediate horsepower and thrust values are determined from the fitted curves at the selected Mach number increments. The routine proceeds until smoothed curves for horsepower (HPI) and thrust (THI), and derived coefficient values plus corresponding RPM and tip speed (TIPS), have been computed at all of the selected increments of Mach number. The procedure is essentially one of creating equal tabular entries through a smoothing technique rather than through an interpolative procedure.

The Namelist variables establish the boundaries of the program, such as the Mach number increments and range, number of data points fitted by the polynomial, and the degree of the polynomial. All variables can be changed to adapt the program to other uses.

SECTION II

COMPUTER PROGRAM

1. PROGRAM OPERATION

The computer program is designed to provide parameters for aircraft propellers at specified tip Mach number increments by fitting curves to data for horsepower and thrust versus Mach number at a set blade angle and re-computing values for the parameters at the predetermined Mach number increments. A flow chart showing the order of the program and the data input is given in Figure 1. Data is obtained from a test rig data sheet, such as is shown in Figure 2, and coded for the computer as shown in Figure 3.

For a given blade angle, the data must be presented to the computer at increasing values of RPM. After receiving the data input, the computer calculates the various parameters from the test data, including Mach number, C_t , C_p , C_t/C_p , F.M., and TH/HP, according to the appropriate equations (given in the list of program variables). Values are printed out on the output sheet, Figure 4, as Raw Data Points.

Subroutine XIPLSQ is then called to fit a 6-point, 2nd order, least squares curve through the data points for HP and TH at test tip Mach numbers. Then the computer determines values for HP and TH from the fitted curves that correspond to the selected Mach numbers, and uses these values to recompute values for all parameters at the selected Mach numbers. These values are then printed out on the output sheet as shown on Figure 4 under Fitted Curve Data for Constant Mach Number Increments.

The computer then reads in the data for a new blade angle (2nd Beta, 3rd Beta, etc.) and repeats the computations.

2. SUBROUTINE XIPLSQ

The least squares curve is fitted by means of Subroutine XIPLSQ. HPI and THI values are computed as functions of the independent variable BMACH by



[illegible]

Figure 2. Typical Rig Data Sheet

FORTRAN CODING FORM									
Program		Punching Instructions				Page 1 of 1			
Programmer		Date		Graphic Punch		Card Form		Identification	
				<input checked="" type="checkbox"/>				73 70 65 60 55 50 45 40 35 30 25 20 15 10 5	
FORTRAN STATEMENT									
1	5	16	17						
2 FFENGA1-4A RUN 23A 7 JAN 66 (PRPP IP CARD) (5)									
(NBL) 4 (AF) (DIA) (TEMP °C) 1.050									
(RPM) 105.0 15.625 12.1 -4.0									
652 372 2762									
702 476 3251									
749 580 3714									
797 723 4314									
848 853 4790									
898 1046 5552									
955 1288 6352									
1003 1519 7105									
1052 1784 7876									
1096 2060 8695									
1148 2486 9838									
1194 2884 10857									
1230 3224 11619									
NOTE: Identifying information in () is not coded.									

Figure 3. Sample Coding Form
(Taken from Typical Rig Data Sheet)

STATIC PROP PERFORMANCE

2FF13A1-4A 7JAN66 RUN 10 230 WALLS DOWN 15000 FT-LR

BETA=12.1 AF= -0. DIA=15.625 NBL=4 TEMPC= -4.0 TEMPR= 486.49 SIGMA=1.0500

***** RAW DATA POINTS *****

RPM	HP	TH	TMACH	RCI	RCP	RCI/CP	RFM	RTM/HP
652.	372.	2762.	0.494	0.1655	0.0721	2.2964	0.7454	7.4247
702.	475.	3237.	0.532	0.1683	0.0739	2.2786	0.7450	6.3424
749.	530.	3714.	0.568	0.1686	0.0741	2.2752	0.7455	6.4034
797.	723.	4314.	0.604	0.1730	0.0767	2.2559	0.7497	5.9658
848.	853.	4790.	0.643	0.1696	0.0751	2.2589	0.7425	5.6155
894.	1049.	5552.	0.681	0.1753	0.0775	2.2611	0.7555	5.3078
955.	1283.	6332.	0.724	0.1774	0.0794	2.2342	0.7509	4.9317
1003.	1517.	7103.	0.760	0.1799	0.0808	2.2255	0.7532	4.6774
1052.	1784.	7876.	0.797	0.1812	0.0823	2.2032	0.7485	4.4148
1096.	2060.	8695.	0.831	0.1843	0.0840	2.1945	0.7519	4.2209
1142.	2435.	9833.	0.870	0.1901	0.0882	2.1551	0.7499	3.9574
1194.	2884.	10837.	0.905	0.1940	0.0910	2.1323	0.7494	3.7646
1230.	3224.	11619.	0.932	0.1956	0.0930	2.1028	0.7421	3.6039

***** FITTED CURVE DATA FOR CONSTANT MACH NUMBER INCREMENTS ***** (HP, 6 POINT 2ND ORDER, TH, 6 POINT 2ND ORDER)

MACH	HP	TH	TIPS	RPM	CT	CP	CT/CP	FM	TH/HP
0.725	1293.	6379.	743.	957.	0.1775	0.0793	2.239	0.753	4.934
0.750	1453.	6892.	810.	990.	0.1793	0.0805	2.227	0.753	4.745
0.775	1615.	7329.	837.	1023.	0.1800	0.0811	2.219	0.751	4.576
0.800	1804.	7956.	864.	1059.	0.1819	0.0823	2.209	0.752	4.411
0.825	2022.	8574.	891.	1088.	0.1843	0.0842	2.190	0.750	4.241
0.850	2262.	9243.	918.	1121.	0.1872	0.0861	2.174	0.750	4.086
0.875	2528.	9934.	944.	1154.	0.1898	0.0882	2.152	0.748	3.930
0.900	2819.	10663.	971.	1187.	0.1926	0.0904	2.131	0.746	3.784
0.925	3134.	11430.	998.	1220.	0.1954	0.0926	2.111	0.745	3.647

Figure 4. Typical Computer Printout

means of a polynomial smoothing process; this process resembles nonlinear interpolation in that it considers several points of the HP and TH versus AMACH tabular data function on either side of the desired BMACH value in determining a least squares polynomial, and this polynomial is then used to determine the smoothed HPI and THI values.

Smoothing in the vicinity of the ends of the test data array will not produce as satisfactory results as in the center because there are not sufficient data points available on both sides of the desired BMACH argument. The polynomial is always fit to the predetermined number of test data points, however, so additional data points from the other side are used to augment the least squares input data. If the desired BMACH value is out of range of the test data, however, extrapolative smoothing would be required, which would give results of even less reliability.

Note that if the fitted polynomial is of the Nth degree, $N + 1$ data points are required to develop the smoothing polynomial.

3. DATA INPUT

The first data input card (propeller identification card) shows which propeller data is being computed. The second card gives the basic propeller data and atmospheric conditions at the time that the test was run, including the number of blades, propeller diameter, activity factor, blade angle setting, temperature ($^{\circ}\text{C}$), and density ratio (air factor). The first RPM value with its corresponding HP and TH values is punched on the third card, and values for increasing RPMs are punched on succeeding cards. A blank card is placed after the last RPM-HP-TH card if another blade angle run is to be computed for that propeller; if no more blade angle runs are to be made, a "-1." card (with -1. punched within the first 10 spaces) follows.

SECTION III PROGRAM PARAMETERS

1. NAMELIST

The variables in the Namelist control various aspects of the program. They are set at specified values by the DATA statement near the beginning of the program deck.

There is one Namelist, NAM, for this program, consisting of the following variables:

- VL = VL + VS, - minimum selected Mach number for curve-fitted data (VL set at 0.500)
- VH - maximum selected Mach number for curve fitted data (VH set at 1.000)
- VS - increment increase in selected Mach numbers (VS set at 0.025)
- NP TH - maximum number of raw thrust points considered at one time for a curve fit (NPHP set at 6)
- NPHP - maximum number of raw horsepower points considered at one time for a curve fit (NPHP set at 6)
- NDTH - order of the polynomial used for fitting the thrust curve. (NDTH is set at 2; that is, a running polynomial of the form $C_0 + C_1 x + C_2 x^2$ is used in smoothing the thrust data unless modified by parameter control.)
- NDHP - see information for NDTH, above (set at 2).

Namelist values can be modified by the simple procedure of replacing one card. For example, if the value for VH (maximum Mach number) is to be changed from 1.000 to 0.900, the following card would be removed

Card Column 2

\$ NAM \$ (the first card after the \$ DATA control card)

and the following card inserted:

Card Column 2

\$ NAM VH = .9\$

2. EQUATIONS

The following equations are used in computing the parameters.

$$TR = 1.8(TC + 273.16)$$

$$AMACH = \left(\frac{\pi}{60}\right) \frac{(RPM) (DIA)}{(49.04) \sqrt{TR}}$$

$$CT = CT(TH) = 0.1518 \times 10^7 \frac{TH}{(RPM)^2 (DIA)^4}$$

$$CTI = CT(THI) \quad (\text{see THI})$$

$$CP = CP(HP) = 0.5 \times 10^{11} \frac{HP}{(RPM)^3 (DIA)^5}$$

$$CPI = CP(HPI) \quad (\text{see HPI})$$

$$FM = FM(CT, CP) = 0.798 \frac{|CT|^{1.5}}{CP} ; \quad \text{if } CT < 0, \text{ FM is set at minus value.}$$

$$FMI = FM(CTI, CPI)$$

3. OTHER PROGRAM VARIABLES

a. Nonsubscripted Variables

NBL - number of blades per propeller (reference data)

AF - activity factor (reference data)

DIA - diameter of propeller, feet

RPM - propeller speed (revolutions per minute)

CT - coefficient of thrust

CP - coefficient of power

FM - Figure of Merit

TIPS - actual tip speed, ft/sec

b. Subscripted Variables

HEAD - propeller identification

B - BETA, blade angle, degrees (reference data)

TC - TEMPC, ambient temperature (°C)

S - "sigma" = (air factor) density ratio (σ)

TR - TEMPR, ambient temperature (°R)

HP - corrected horsepower; (Corrected HP = $\frac{\text{Test HP}}{\sigma}$)

TH - corrected thrust, pounds (Corrected TH = $\frac{\text{Test TH}}{\sigma}$)

AMACH - actual tip Mach number

BMACH - selected Mach number for curve fit

THI - thrust values determined from the smoothed thrust curve.

HPI - horsepower values determined from the smoothed horsepower curve.

FMI - interpolated figure of merit

CTI - interpolated coefficient of thrust

CPI - interpolated coefficient of power

c. Counters

NP - number of propellers

NB - number of blade angles

N - number of cards per blade angle run

NV-J-1 - number of selected Mach numbers per run

d. Miscellaneous Parameters

$$AF - \text{activity factor} = \frac{100,000}{16} \int_{0.2}^{1.0} \frac{b}{DIA} \left(\frac{r}{R} \right)^3 d \left(\frac{r}{R} \right)$$

b - blade width, feet

R - total blade radius, feet

r - radius along blade, feet

σ - density ratio; $\sigma = \frac{\rho}{\rho_0}$ (reference data)

ρ - local density, lb sec²/ft⁴

ρ_0 - sea level standard density, lb sec²/ft⁴

SECTION IV

COMPARISON OF CURVES

A comparison of the computer curve-fit data with hand-faired data for thrust and horsepower is shown in Figures 5 and 6. These figures show that the test data and the computer curve-fit provide very good agreement. The curve-fit results in a substantial smoothing of the data.

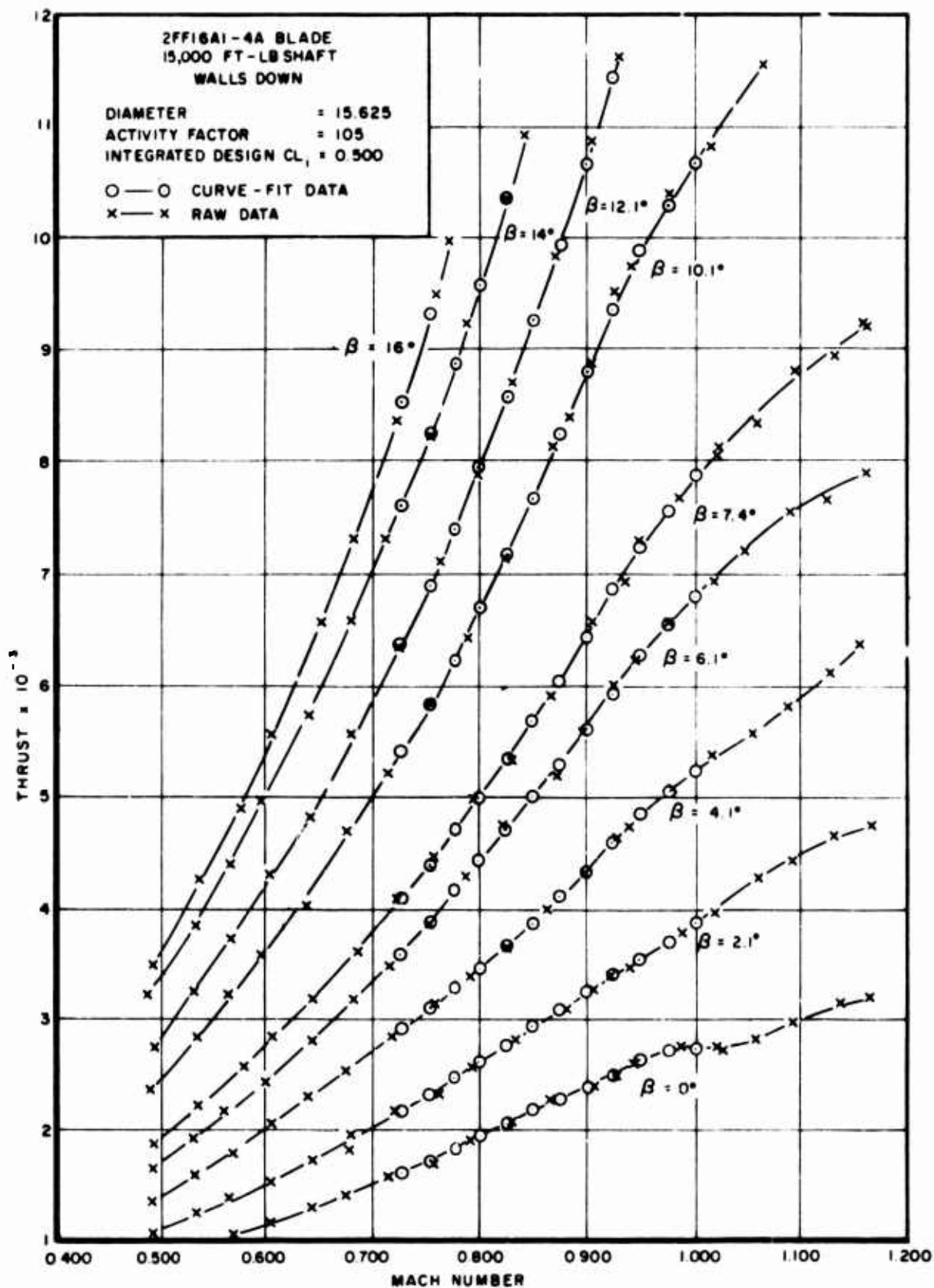


Figure 5. Comparison of Thrust Curve-Fit Data to Raw Data

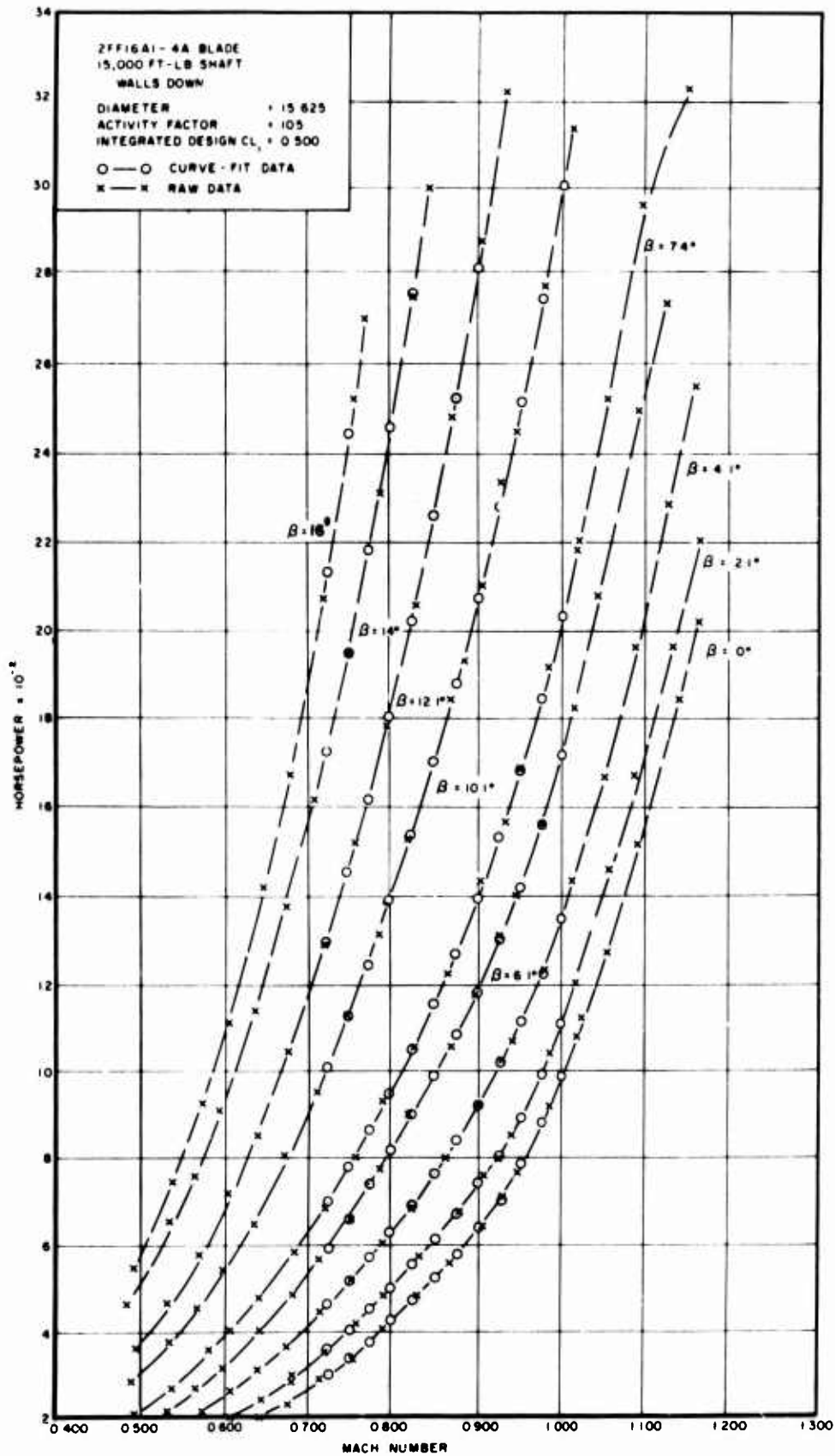


Figure 6. Comparison of Horsepower Curve-Fit Data to Raw Data

APPENDIX

COMPUTER PROGRAM

This appendix presents the basic computer program and the necessary subroutines, followed by an explanation of the subroutines.

```

C IRJOB PROP MAP
C IBFTC CHOPN DECK
  DIMENSION HEAD(13),B(30),TC(30),S(30),TR(30),HPI(30),TH(30),
  1 AMACH(30),EMACH(60,60),THI(60),HPI(60),FMI(60,60),
  2 CTI(60,60),CPI(60,60)
  DATA ZC/273.16/,COFT/49.04/,COFCT/.1518E7/,COFCP/.5E11/,
  1 COFFMA.798/VL/.5/,VH/1./,VS/.025/,NP/6/,NPHP/6/,
  2 NDTH/2/,NDHP/2/,LIST/0/
  NAMELIST/NAM/VL,VH,VS,NPTH,NPHP,NDTH,NDHP,LIST
C NAMELIST NAM PARAMETERS,
C VL(VS)VH = LOW, STEP, HIGH, MACH NUMBER TABULAR INTERVAL (SMOOTHED),
C NPTH, NPHP = NUMBER OF POINTS USED IN SMOOTHING THRUST, HORSEPOWER,
C NDTH, NDHP = DEGREE OF POLYNOMIAL USED IN SMOOTHING TH AND HP.
C LIST = 0,1 LEAST SQUARES ANALYSIS NOT USED (0), USED (1).
  PIO60=4.*DATAN(1.00)/60.
  10 READ(5,NAM)
  NP=0
  15 NP=NP+1
  DO 20 K=1,30
  DO 20 L=1,30
  CTI(K,L)=0.
  20 CPI(K,L)=0.
  NR=0
  25 NB=NB+1
  READ(5,30)(HEAD(J),J=1,13)
  30 FORMAT(13A6)
  READ(5,35)NBL,AF,DIA,B(NB),TC(NB),S(NB)
  35 FORMAT(110,5F10.5)
  TR(NB)=1.8*(TC(NB)+ZC)
  WRITE(6,40)(HEAD(J),J=1,13),B(NB),AF,DIA,NBL,TC(NB),TR(NB),S(NB)
  40 FORMAT(24H1STATIC PROP PERFORMANCE/////1H0,13A6/7H0 BETA=F4.1,
  14H AF=,
  2 F5.1,5H DIA=F6.3,5H NBL=,11,7H TEMPC=F5.1,7H TEMPR=F7.2,
  3 7H SIGMA=F6.4)
  WRITE(6,45)
  45 FORMAT(28H0***** RAW DATA POINTS *****/
  1 1H0,7X,3HRPM,4X,2HHP,4X,2HTH,1X,5HTMACH,7X,3HRCI,7X,3HRCP,4X,
  2 6HRCI/CP,7X,3HRFM,4X,6HRTTH/HP)
  N=0
  50 N=N+1
  READ(5,55)RPM,HP(N),TH(N)
  55 FORMAT(3F10.1)
  TEST=RPM
  IF(TEST.LE.0.) GO TO 75
  AMACH(N)=(PIO60*RPM*DIA)/(COFT*SQRT(TR(NB)))
  CT=COFCT*TH(N)/(RPM**2*DIA**4)

```

```

CP=COFCP*HP(N)/(RPM**3*DIA**5)
CTOCP=CT/CP
FM=COFFM*SIGN(ABS(CT)**1.5,CT)/CP
THOHP=TH(N)/HP(N)
WRITE(6,70)RPM,HP(N),TH(N),AMACH(N),CT,CP,CTOCP,FM,THOHP
70  FORMAT(5X,3F6.0,F6.3,5F10.4)
    GO TO 50
75  N=N-1
    WRITE(6,80)NPHP,NDHP,NPTH,NDTH
    FORMAT(66H0***** FITTED CURVE DATA FOR CONSTANT MACH NUMBER
80  1 INCREMENTS *****5H (HP,12.6H POINT,12,14HND ORDER. TH,12,
    2 6H POINT,12,9HND ORDER)/
    3      1H0,6X,4HMACH,5X,2HHP,5X,2HTH,3X,4HTIPS,4X,
    4 3HRPM,6X,2HCT,5X,2HCP,2X,5HCT/CP,5X,2HEM,2X,5HTH/HP)
    J=0
    STEP=0.
82  J=J+1
83  STEP=STEP+1.
    BMACH(J,NB)=VL+STEP*VS
    IF(BMACH(J,NB).LT.AMACH(1)) GO TO 83
    IF(BMACH(J,NB).GT.AMACH(N).OR.BMACH(J,NB).GT.VH) GO TO 90
    CALL XIPLSQ(AMACH,HP,BMACH(J,NB),HPI(J),
    1 N,MINO(N,NPHP),NDHP,LIST,LE)
    CALL XIPLSQ(AMACH,TH,BVACH(J,NB),THI(J),
    1 N,MINO(N,NPTH),NDTH,LIST,LE2)
    TIP=BMACH(J,NB)*COFT*SQRT(TR(NB))
    RPM=TIP/(PI*60*DIA)
    CTI(J,NB)=COFCT*THI(J)/(RPM**2*DIA**4)
    CPI(J,NB)=COFCP*HPI(J)/(RPM**3*DIA**5)
    CTOCP=CTI(J,NB)/CPI(J,NB)
    FMI(NB,J)=COFFM*SIGN(ABS(CTI(J,NB)**1.5,CTI(J,NB))/CPI(J,NB)
    THOHP=THI(J)/HPI(J)
    WRITE(6,85)BMACH(J,NB),HPI(J),THI(J),TIP,RPM,CTI(J,NB),
    1 CPI(J,NB),CTOCP,FMI(NB,J),THOHP
85  FORMAT(5X,F6.3,4F7.0,F8.4,F7.4,3F7.3)
    GO TO 82
90  NV=J-1
95  IF(TEST.EQ.0.) GO TO 25
110 IF(TEST.FQ.-1.) GO TO 15
    GO TO 10
END

```



```

*IRFTC XYPLSQ  DECK
SUBROUTINE XYPLSQ (X,Y,XI,YI,N,NP,LD,LIST,LE)
DIMENSION X(1),Y(1),C(11)
LE=0
LD1=LD+1
IF (N) 1,1,2
1  LE=1
   RETURN
2  IF (NP) 3,3,4
3  LE=2
   RETURN
4  IF (N-NP) 5,6,6
5  LE=2
   RETURN
6  IF (X(1)-X(N)) 7,7,8
7  DO 11 I=1,N
   K1=I
   IF (X(I)-X1) 11,12,10
11 CONTINUE
   GO TO 14
8  DO 13 I=1,N
   K1=N
   IF (X(I)-X1) 10,12,13
13 CONTINUE
14 K1=N+1-NP
   GO TO 17
10 K1=K1-1
12 K1=K1-(NP-1)/2
   IF (K1) 9,9,15
   K1=1
   GO TO 17
15 IF (K1+NP-1-N) 17,17,16
16 K1=N+1-NP
17 CALL PLSQ (X(K1),Y(K1),NP,LD,C,LIST,EMAX,ERMS,EMEQ),
   YI=C(1)
   DO 18 I=2,LD1
18 YI=YI*X1+C(I)
   RETURN
END

```

```

C      $IRFTC MTXEQ.  DECK
C      SUBROUTINE MTXEQ(A,X,B,N,K)
C      MATRIX EQUATION SOLVER      (7094 FORTRAN IV)
C      USAGE...
C      TO SOLVE THE LINEAR SYSTEM      AX=B
C      CALL MTXEQ(A,X,B,N,K)
C      WHERE A MUST BE DIMENSIONED N X N
C      X MUST BE DIMENSIONED N X K
C      B MUST BE DIMENSIONED N X K
C      N IS THE NO. OF EQUATIONS (ROWS IN A,X,B)
C      K IS THE NO. OF SOLUTION VECTORS (COLS. IN X,B)
C      664 CELLS OF BLANK COMMON ARE USED.
C      NOTE... TO CHANGE DIMENSIONS OF ARRAYS C AND PIV, ALSO
C      CHANGE VALUES OF NMAX AND NKMAX IN DATA STATEMENT.
C      DIMENSION A(N,N), B(N,K), X(N,K)
C      COMMON ATPE, I, IFROM, IPI, IPIV, ITO,
C      J, KP, L, NP, NPI, NPJ, NPK, RM
C      COMMON PIV(26), C(24,26)
C      DATA NMAX, NKMAX/ 24, 26/
C      TEST N AND K FOR CORRECT RANGE
C      IF ( N .LE. 0 .OR. N .GT. NMAX ) GO TO 190
C      IF ( K .LE. 0 .OR. (N+K) .GT. NKMAX ) GO TO 190
C      GET ARGUMENTS N AND K
C      NP=N
C      KP=K
C      MOVE ARRAYS A(I,J) AND B(I,J) INTO C(I,J)
C      DO 10 J=1,NP
C      DO 10 I=1,NP
C      C(I,J)=A(I,J)
C      DO 20 J=1,KP
C      NPJ=NP+J

```

MTXEQ001
 MTXEQ002
 MTXEQ003
 MTXEQ004
 MTXEQ005
 MTXEQ006
 MTXEQ007
 MTXEQ008
 MTXEQ009
 MTXEQ010
 MTXEQ011
 MTXEQ012
 MTXEQ013
 MTXEQ014
 MTXEQ015
 MTXEQ016
 MTXEQ017
 MTXEQ018
 MTXEQ019
 MTXEQ020
 MTXEQ021
 MTXEQ022
 MTXEQ023
 MTXEQ024
 MTXEQ025
 MTXEQ026
 MTXEQ027
 MTXEQ028
 MTXEQ029
 MTXEQ030
 MTXEQ031
 MTXEQ032
 MTXEQ033
 MTXEQ034
 MTXEQ035
 MTXEQ036
 MTXEQ037
 MTXEQ038
 MTXEQ039
 MTXEQ040
 MTXEQ041
 MTXEQ042
 MTXEQ043
 MTXEQ044
 MTXEQ045

```

MTXEQ046
MTXEQ047
MTXEQ048
MTXEQ049
MTXEQ050
MTXEQ051
MTXEQ052
MTXEQ053
MTXEQ054
MTXEQ055
MTXEQ056
MTXEQ057
MTXEQ058
MTXEQ059
MTXEQ060
MTXEQ061
MTXEQ062
MTXEQ063
MTXEQ064
MTXEQ065
MTXEQ066
MTXEQ067
MTXEQ068
MTXEQ069
MTXEQ070
MTXEQ071
MTXEQ072
MTXEQ073
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MTXEQ076
MTXEQ077
MTXEQ078
MTXEQ079
MTXEQ080
MTXEQ081
MTXEQ082
MTXEQ083
MTXEQ084
MTXEQ085
MTXEQ086
MTXEQ087
MTXEQ088
MTXEQ089
MTXEQ090
MTXEQ091

DO 20 I=1,NP
  C(I,NPJ)=B(I,J)
  C
  SET TO PERFORM N ELIMINATION SWEEPS (I=1,N)
  C
  NP1=NP+1
  NPK=NP+KP
  DO 120 I=1,NP
    IPI=I+1
    C
    SEARCH FOR NEXT PIVOT ROW (I-TH PIVOT IS IN COL. I)
    C
    ATPE=0.
    DO 40 J=I,NP
      IF (ABS(C(J,I))-ATPE) 40,30,30
      ATPE=ABS(C(J,I))
      IPIV=J
    30 CONTINUE
    C
    OPERATE ON THE PIVOT ROW
    C
    IF (ATPE) 210,210,50
    DO 60 J=IPI,NPK
      PIV(J)=C(IPIV,J)/C(IPIV,I)
    50
    60
    C
    PERFORM ELIMINATIONS BELOW THE DIAGONAL (COL. I)
    C
    IFROM=NP
    ITO=NP
    IF (IFROM-IPIV) 80,100,80
    70 RM=-C(IFROM,I)
    80 DO 90 J=IPI,NPK
      C(ITO,J)=C(IFROM,J)+RM*PIV(J)
    90 ITO=ITO+1
    100 IFROM=IFROM+1
      IF (IFROM-I) 110,70,70
    C
    PUT THE I-TH PIVOT ROW IN THE VACATED ROW I
    C
    DO 120 J=IPI,NPK
    110 C(I,J)=PIV(J)
    120
    C
    NOW DO THE BACK SOLUTION
    C
    I=NP
    IPI=I
    130

```



```

SIBFTC PLSQ.  DECK
SUBROUTINE PLSQ(X,Y,N,K,C,LIST,EMAX,ERMS,EMEQ)
C
C      PLSQ      POLYNOMIAL LEAST SQUARE CURVE FIT
C
C      PLSQ WILL FIT A GIVEN SET OF DATA TO A
C      POLYNOMIAL OF DEGREE K OF THE FORM...
C      
$$Y = C(K+1) + C(K) * X + C(K-1) * X^2 + \dots + C(2) * X^{K-1} + C(1) * X^K$$

C
C      PLSQ THEN COMPUTES THE MAXIMUM ERROR AND ROOT
C      MEAN SQUARE ERROR OBTAINED BY USING THE C
C      COEFFICIENTS TO RE-COMPUTE Y FROM X
C
C      USAGE...
C
C      DIMENSION X(N), Y(N), C(L)
C      WHERE L IS K+1
C      CALL PLSQ(X,Y,N,K,C,LIST,EMAX,ERMS,EMEQ)
C
C      WHERE,
C
C      X  IS THE ARRAY OF N INDEPENDENT VARIABLES
C
C      Y  IS THE ARRAY OF N DEPENDENT VARIABLES
C
C      N  IS THE NUMBER OF INDEPENDENT(DEPENDENT)
C      VARIABLES
C
C      K  IS THE DEGREE OF THE LEAST SQUARES POLYNOMIAL
C
C      C  IS THE ARRAY OF THE COEFFICIENTS,HIGH ORDER
C      TO LOW ORDER, OF THE LEAST SQUARES POLYNOMIAL
C
C      LIST = 0  SUPPRESSES THE ERROR ANALYSIS OUTPUT
C      LIST = 1  GIVES THE ERROR ANALYSIS OUTPUT
C
C      EMAX  IS THE MAXIMUM ABSOLUTE ERROR OBTAINED
C      BY USING THE COMPUTED C COEFFICIENTS TO
C      APPROXIMATE THE DEPENDENT VARIABLE
C
C      ERMS  IS THE ROOT MEAN SQUARE ERROR OBTAINED
C      BY USING THE COMPUTED C COEFFICIENTS TO
C      APPROXIMATE THE DEPENDENT VARIABLE
C
C
C

```

PLSQ0001
 PLSQ0002
 PLSQ0003
 PLSQ0004
 PLSQ0005
 PLSQ0006
 PLSQ0007
 PLSQ0008
 PLSQ0009
 PLSQ0010
 PLSQ0011
 PLSQ0012
 PLSQ0013
 PLSQ0014
 PLSQ0015
 PLSQ0016
 PLSQ0017
 PLSQ0018
 PLSQ0019
 PLSQ0020
 PLSQ0021
 PLSQ0022
 PLSQ0023
 PLSQ0024
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 PLSQ0028
 PLSQ0029
 PLSQ0030
 PLSQ0031
 PLSQ0032
 PLSQ0033
 PLSQ0034
 PLSQ0035
 PLSQ0036
 PLSQ0037
 PLSQ0038
 PLSQ0039
 PLSQ0040
 PLSQ0041
 PLSQ0042
 PLSQ0043
 PLSQ0044
 PLSQ0045

```

C      EMEQ  IS THE MAXIMUM DEVIATION FROM UNITY
C      IN THE LINEAR SYSTEM CHECK SOLUTION
C
C
C      PLSQ CALLS SUBROUTINE MTXEQ
C
C      PLSQ USES 1309 CELLS OF BLANK COMMON
C
C      COMMON  MTXEQT(664), CF, DIF, I, J, JC, JK,
C      *      L, LL, LU, M, SUM, XI, XM(576),
C      *      XMAX, XMIN, XP, YC, YM(48)
C      DIMENSION  X(N), Y(N), C(24),
C      *      XDP(48), XYDP(24)
C      EQUIVALENCE  (MTXEQT(1),XDP(1)), (MTXEQT(97),XYDP(1))
C      LOGICAL  LIST
C      DOUBLE PRECISION  CF, XDP, XI, XMAX, XMIN, XP, XYDP
C      DATA  KMAX/ 23/..
C
C      CHECK K AND N FOR PROPER RANGE
C
C      IF (K .GT. KMAX .OR. N .LE. K .OR. K .LE. 0)  GO TO 200
C      L=K+1
C
C      FIND MINIMUM AND MAXIMUM VALUES FOR X
C
C      XMIN=X(1)
C      XMAX=X(1)
C      DO 10 I=2,N
C      XMIN=AMIN1(XMIN,X(I))
C      XMAX=AMAX1(XMAX,X(I))
C
C      ZERO DOUBLE PRECISION ARRAYS FOR SUMMING
C
C      M=2*K+1
C      DO 20 I=1,M
C      XDP(I)=0.0D+00
C      DO 25 I=1,L
C      XYDP(I)=0.0D+00
C
C      TRANSFORM RANGE OF X TO (-1,+1) AND
C      COMPUTE SUMS OF POWERS OF X AND SUMS
C      OF Y TIMES POWERS OF X
C
C      LL=K+2
C      LU=2*K+1

```

PLSQ0046
PLSQ0047
PLSQ0048
PLSQ0049

PLSQ0051
PLSQ0052
PLSQ0053
PLSQ0054
PLSQ0055
PLSQ0056
PLSQ0057
PLSQ0058
PLSQ0059

PLSQ0060
PLSQ0061
PLSQ0062
PLSQ0063
PLSQ0064
PLSQ0065
PLSQ0066
PLSQ0067
PLSQ0068
PLSQ0069

PLSQ0070
PLSQ0071
PLSQ0072
PLSQ0073
PLSQ0074
PLSQ0075
PLSQ0076
PLSQ0077
PLSQ0078
PLSQ0079

PLSQ0080
PLSQ0081
PLSQ0082
PLSQ0083
PLSQ0084
PLSQ0085
PLSQ0086
PLSQ0087
PLSQ0088
PLSQ0089

PLSQ0090
PLSQ0091


```

DO 40 I=1,N
XP=1.0D+00
XI=2.0D+00*(X(I)-XMIN)/(XMAX-XMIN)-1.0D+00
DO 30 J=1,L
XDP(J)=XDP(J)+XP
XYDP(J)=XYDP(J)+XP*Y(I)
XP=XP*XI
30
DO 40 J=LL,LU
XDP(J)=XDP(J)+XP
XP=XP*XI
40
C
C STORE ABOVE COMPUTED SUMS IN ARRAY XM
C AND COMPUTE ROW SUMS FOR CHECK SOLUTION
C
DO 50 I=1,L
LL=I+L
YM(LL)=0.0
LU=(I-1)*L
JK=I-1
DO 50 J=1,L
JK=JK+1
JC=LU+J
XM(JC)=XDP(JK)
50
YM(LL)=YM(LL)+XM(JC)
DO 60 I=1,L
60
YM(I)=XYDP(I)
C
C SOLVE THE SYSTEM XM*C=YM
C
C CALL MTXEQ(XM,YM,YM,L,2)
C
C REORDER AND MOVE SOLUTION TO C AND FIND
C MAXIMUM ERROR IN CHECK SOLUTION
C
EMEQ=0.0
DO 70 I=1,L
JK=K-I+2
C(JK)=YM(I)
70
JC=I+L
EMEQ=AMAX1(EMEQ,ABS(YM(JC)-1.0))
C
C ADJUST COEFFICIENTS FOR ORIGINAL RANGE
C OF X
C
CF=(XMAX-XMIN)/2.0D+00
DO 80 I=1,K
80

```

```

PLSQ0092
PLSQ0093
PLSQ0094
PLSQ0095
PLSQ0096
PLSQ0097
PLSQ0098
PLSQ0099
PLSQ0100
PLSQ0101
PLSQ0102
PLSQ0103
PLSQ0104
PLSQ0105
PLSQ0106
PLSQ0107
PLSQ0108
PLSQ0109
PLSQ0110
PLSQ0111
PLSQ0112
PLSQ0113
PLSQ0114
PLSQ0115
PLSQ0116
PLSQ0117
PLSQ0118
PLSQ0119
PLSQ0120
PLSQ0121
PLSQ0122
PLSQ0123
PLSQ0124
PLSQ0125
PLSQ0126
PLSQ0127
PLSQ0128
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PLSQ0130
PLSQ0131
PLSQ0132
PLSQ0133
PLSQ0134
PLSQ0135
PLSQ0136
PLSQ0137

```


EXPLANATION OF
SUBROUTINE MTXEQ

MTXEQ, Matrix Equation Solver, solves the system of linear equations expressed by the matrix equation $AX = B$, using single precision floating arithmetic.

Control:

To solve the matrix equation,

$$AX = B$$

the following calling sequence is used:

```
DIMENSION A(N,N), X(N,K), B(N,K)
CALL MTXEQ(A,X,B,N,K)
```

where

A - is the N by N coefficient matrix. The A matrix is not destroyed.

X - will be the N by K solution matrix.

B - is the N by K right-hand-side matrix. The B matrix is not destroyed.

N - is the number of equations, i.e., rows in A, X and B.
($1 \leq N \leq 24$)

K - is the number of solution, i.e., columns in X and B.
($K > 0$ and $(N+K) \leq 26$)

Other Programming Information:

1. Other subprograms used - None.

2. Error conditions -

- a. The following ranges of N and K are allowed:

$$(1 \leq N \leq 24)$$

$$K > 0 \text{ and } (N+K) \leq 26$$

When violations of the above ranges are detected by MTXEQ, a message is written and FXEM is called. The upper limits on N and (N+K) may be altered by changing a DIMENSION and a DATA statement.

- b. If the A matrix has $\text{DET}(A) = 0$, a message is written and FXEM is called.

- c. Common usage -

MTXEQ uses 664 cells of blank common.

Method:

The matrix $C = [A, B]$ is formed in blank common. Subsequent operations are performed on the C matrix, thus preserving the A and B matrices. Elementary row operations are performed to eliminate elements below the main diagonal of the augmented matrix C. To reduce the propagation of round-off error, the i-th pivot element is chosen to be an element having maximum magnitude in the i-th sub-column. Finally, a back solution gives the desired matrix, X. The number of floating point arithmetic operations required using this method is of the order of $2/3 (N^3 + 3KN^2)$.

EXPLANATION OF SUBROUTINE PLSQ

PLSQ, Polynomial Least Square Curve Fit, will fit a given set of data to a polynomial of degree K of the form:

$$Y = C_1 X^k + C_2 X^{k-1} + \dots + C_k X + C_{k+1}$$

An error analysis of the fit is optionally given.

Control:

DIMENSION X(N), Y(N), C(L)

where L is K+1

CALL PLSQ(X,Y,N,K,C,LIST,EMAX,ERMS,EMEQ)

where

X is the array of N independent variables.

Y is the array of dependent variables.

N is the number of independent (dependent) variables.

K is the degree of the least squares polynomial.

C is the array of the coefficients, high order to low order, of the least squares polynomial.

LIST = 0 suppresses the error analysis output.

= 1 gives the error analysis output.

EMAX is the maximum absolute error obtained by using the computed C coefficients to approximate the dependent variable.

ERMS is the root mean square error obtained by using the computed C coefficients to approximate the dependent variable.

EMEQ is the maximum deviation from unity in the linear system check solution.

Other Programming Information:

1. Other subroutines used:

PLSQ calls MTXEQ to solve the normal equations and
FXEM for return to the system on error conditions.

2. Error conditions:

PLSQ checks for the following errors:

- a. $K > 23$
- b. $N \leq K$
- c. $K \leq 0$

Upon detecting an error a pertinent message is given
and FXEM is called for error tracing and return to
the system.

3. Common usage:

PLSQ uses 1309 cells of blank common.

Method:

PLSQ fits a set of observed data, $[x_i, y_i]$, with a polynomial of the form:

$$Y = C_1 X^k + C_2 X^{k-1} + \dots + C_k X + C_{k+1}$$

by solving the normal equations for the C_i 's. A transformation of the range of
X to (-1,1) gives a partial decoupling of the normal equations which improves
the accuracy of the solution. Double precision arithmetic is performed at
critical points in the computation.

UNCLASSIFIED

Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author)		2a. REPORT SECURITY CLASSIFICATION	
Deputy for Engineering Aeronautical Systems Division Wright-Patterson Air Force Base, Ohio		UNCLASSIFIED	
3. REPORT TITLE		2b. GROUP	
COMPUTER PROGRAM FOR REDUCING STATIC PROPELLER TEST DATA			
4. DESCRIPTIVE NOTES (Type of report and inclusive dates)			
5. AUTHOR(S) (First name, middle initial, last name)			
Cafarelli, Gerald T. Chopin, Matthew H.			
6. REPORT DATE	7a. TOTAL NO. OF PAGES	7b. NO. OF REFS	
June 1968	41	0	
8a. CONTRACT OR GRANT NO.	9a. ORIGINATOR'S REPORT NUMBER(S)		
b. PROJECT NO. 478A	ASD-TR-68-19		
c.	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)		
d.			
10. DISTRIBUTION STATEMENT			
This document has been approved for public release and sale; its distribution is unlimited.			
11. SUPPLEMENTARY NOTES		12. SPONSORING MILITARY ACTIVITY	
		Deputy for Engineering Wright-Patterson Air Force Base, Ohio 45433	
13. ABSTRACT			
<p>A computer program using a curve-fit technique was developed to reduce performance data obtained from static tests of aircraft propellers. The entire program is written in Fortran IV language for use on the IBM 7094 computer, located at Wright-Patterson AFB, Ohio.</p> <p>The program accepts static whirl rig test data (ie, raw RPM, horsepower, and thrust data) obtained at a fixed blade angle and reduces it into pertinent propeller relationships. The program first reduces the test data into various coefficients and computes the propeller tip Mach number. A curve fit technique then fits running curves through the test thrust and horsepower data points at the test tip Mach numbers. Intermediate horsepower and thrust values are determined from the fitted curves at selected Mach number increments, and all coefficients are recomputed. This results in a presentation of the reduced data in two forms, coefficients computed from the actual test data and coefficients obtained at specific constant Mach number increments from the fitted curves. The data is presented in tabular printout form. This is a general program and is written so that the order of the curve fit, the Mach number increment, the number of test data points and the Mach number range can be varied.</p> <p>The entire program deck and all nonstandard subroutines are included. Detail instructions are provided which should allow the program to be used by technicians or students who are familiar with Fortran IV language.</p>			

DD FORM 1473
1 NOV 65

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Security Classification

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Security Classification

14	KEY WORDS	LINK A		LINK B		LINK C	
		ROLE	WT	ROLE	WT	ROLE	WT
	Computer Program						
	Aircraft Propeller						
	Static Tests						
	Data Reduction						

UNCLASSIFIED

Security Classification